

A look through the lens



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Functional programming

- Declarativity (laziness, higher-order functions)
- Immutability
- Referential transparency (pure functions)

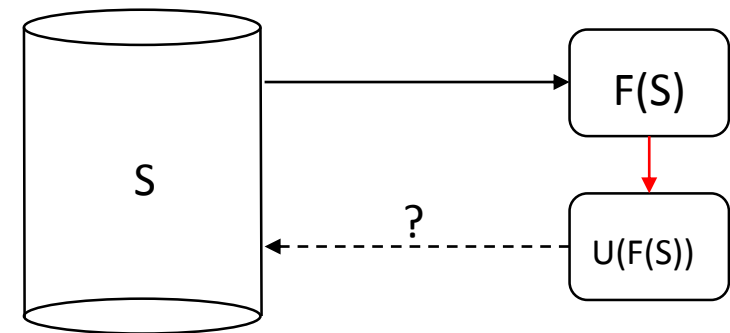
Immutability

- Easier reasoning – no hidden state
- Safer and cleaner concurrent programming
- Better caching



View update problem

- First formulated by E. Codd in 1974
- Some database object S
- Mapped into view state $F(S)$
- View state is changed to $U(F(S))$
- How to translate back $T(U)(S)$?



Bidirectional Programming

- Let's invent a new style of programming
- Programs that can be run “backwards”
- Interfaces and implementations
- Sources and views

- Pierce & Foster's *Harmony/Boomerang*
- *Augeas* config manager (has bindings for *Puppet* and *SaltStack*)

Intermission - Purescript

- Haskell-like statically typed functional language
- Compiles to JS
- Strict evaluation
- Explicit `forall`s (\forall)
- Row types & row polymorphism

```
> let showPerson { first: x, last : y } = y ++ ", " ++ x
```

```
> :type showPerson
```

```
 $\forall$  r. { first :: String, last :: String | r } -> String
```

- Effects instead of IO monad



Bidirectional Programming

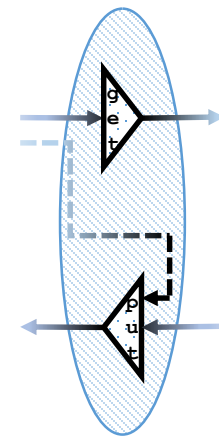
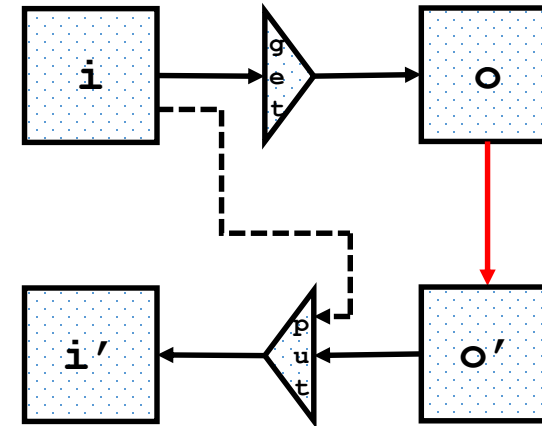
Bijectionness is too strong!

get :: $\forall I O. I \rightarrow O$

put :: $\forall I O. O \rightarrow I \rightarrow I$

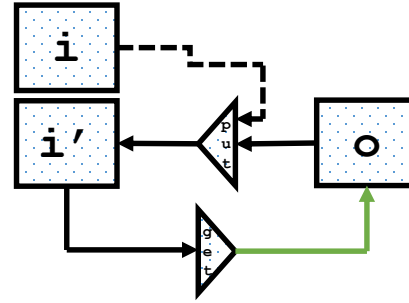
Defining `get` and `put` simultaneously:

- Infer `put` from `get` somehow
- Provide `put+get` pairs as building blocks \leftarrow *lenses*
(we need a type system to help us)

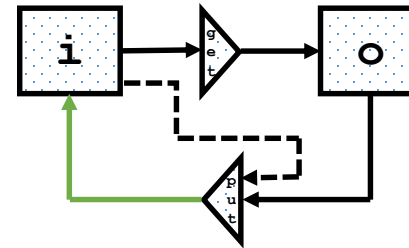


Some laws

1. $\text{get } (\text{put } o \ i) = o$



2. $\text{put } (\text{get } i) \ i = i$

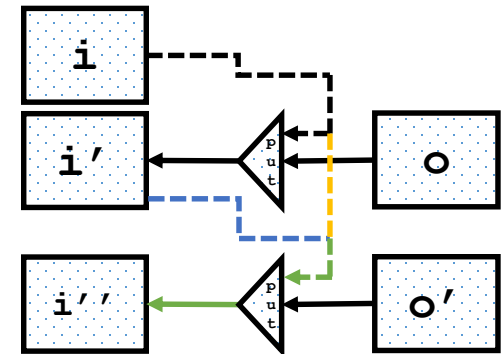


3. $\text{put } o' \ (\text{put } o \ i) = \text{put } o' \ i$

(last put “wins”/no side effects)

Together with 2nd law it means that updates can be “undone”

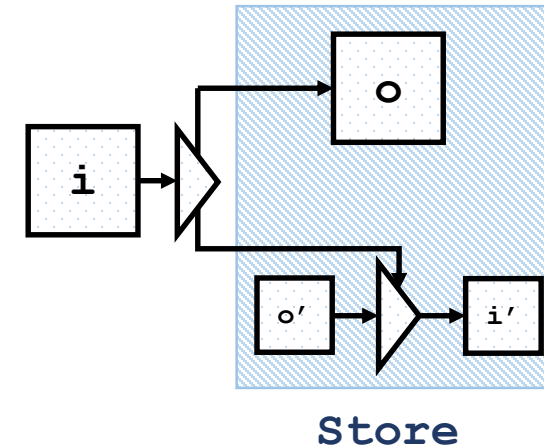
$\text{put } (\text{get } i) \ (\text{put } o \ i) = i$



Approach #1 – Store

Let's change the notation a bit

Lens $i\ o = (i \rightarrow o, o \rightarrow i \rightarrow i)$
 $(i \rightarrow o, i \rightarrow o \rightarrow o)$
 $i \rightarrow (o, o \rightarrow i)$



This is a functor (over i):

$\text{fmap } f \text{ (Store piece hole) = Store piece (f } \lll \text{ hole)}$

It is also a *comonad*...

Intermission - comonads

Monad

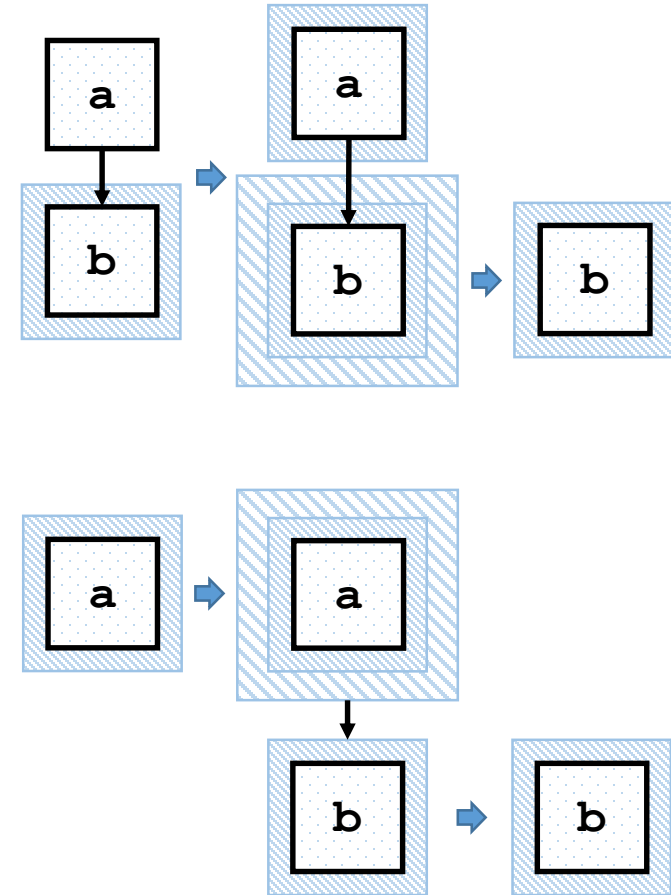
return $:: \forall m\ a. a \rightarrow m\ a$
join $:: \forall m\ a. m\ (m\ a) \rightarrow m\ a$

+laws

Comonad

extract $:: \forall w\ a. w\ a \rightarrow a$
duplicate $:: \forall w\ a. w\ a \rightarrow w\ (w\ a)$

+laws



Useful for manipulating things that are “endless” or “in a context”

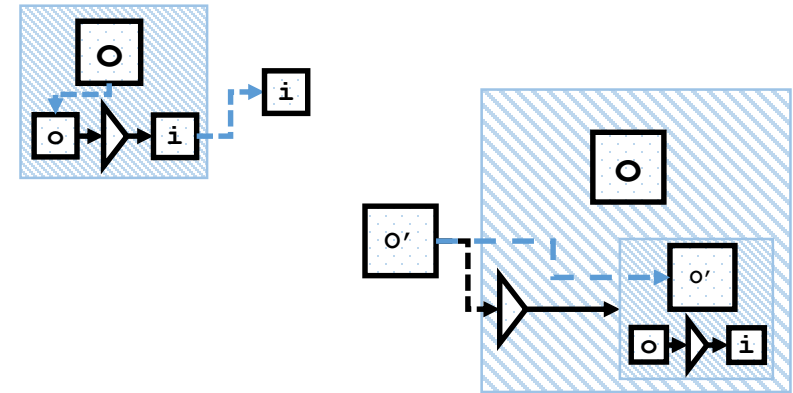
Approach #1 – Store

Going back to Store...

...It is also a *comonad*:

extract (**Store** piece hole) = hole piece

duplicate (**Store** piece hole) =
Store piece (\piece' -> **Store** piece' hole)



In category theory, a functor F with a function $a \rightarrow F a$ (+laws) is called
F-coalgebra

Turns out our Lens type $i \rightarrow (o, o \rightarrow i)$ is a
coalgebra for a Store comonad

aka *O'Connor lenses*

Usage - records

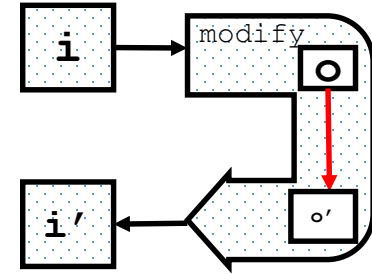
```
petrIvanov :: Person
petrIvanov = Person {
  firstName: "Petr" ,
  lastName: "Ivanov" ,
  address: Address {
    street: StreetRec {
      number: 12 ,
      streetName: "Lenina" ,
      designation: Street
    } ,
    city: "Minsk" ,
    country: Belarus
  }
}
```

Problems

- Not easily composable
- Not too efficient
- Can't change the type after modification

Approach #2 – Modify

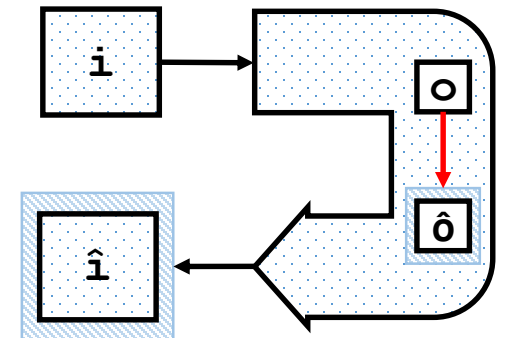
modify :: $\forall I O. (O \rightarrow O) \rightarrow I \rightarrow I$
`modify f i = put (f (get i)) i`



type Lens $I \hat{I} O \hat{O} =$

$\forall F. (\text{Functor } F) \Rightarrow (O \rightarrow F \hat{O}) \rightarrow I \rightarrow F \hat{I}$

aka *van Laarhoven lenses*

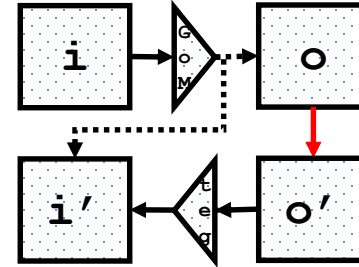


The Zoo

- Prism

`getOrModify` $:: \forall I O. I \rightarrow \text{Either } I O$

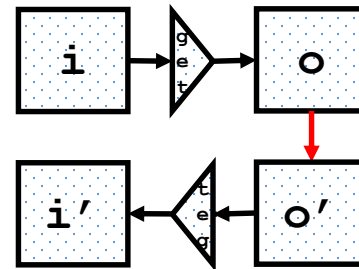
`reverseGet` $:: \forall I O. O \rightarrow I$



- Iso

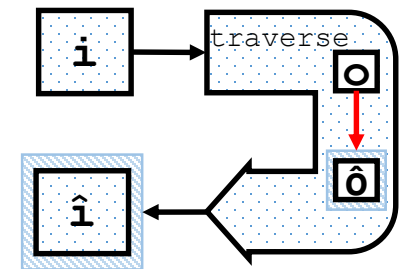
`get` $:: \forall I O. I \rightarrow O$

`reverseGet` $:: \forall I O. O \rightarrow I$



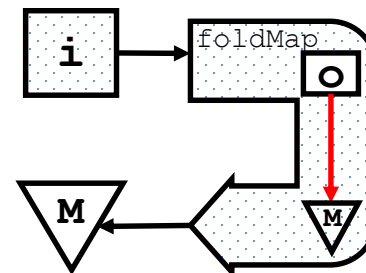
- Traversal

`traverse` $:: \forall F I O. (\text{Applicative } F) \Rightarrow (O \rightarrow F O) \rightarrow I \rightarrow F I$



- Fold

`foldMap` $:: (\text{Monoid } M) \Rightarrow (O \rightarrow M) \rightarrow I \rightarrow M$



Usage – traversals & prisms

```
foo :: Array (Tuple  
              (Either Int (Maybe String))  
              (Maybe Boolean)  
            )
```

```
foo = [  
      Tuple (Left 1) Nothing ,  
      Tuple (Left 2) (Just true) ,  
      Tuple (Right (Just "three")) (Just true) ,  
      Tuple (Right (Just "four")) (Just false) ,  
      Tuple (Right Nothing) Nothing  
    ]
```


Approach #3 – Profunctor

```
class Profunctor p where
```

```
  dimap :: ∀ a b c d. (a -> b) -> (c -> d) -> p b c -> p a d
```

```
class (Profunctor p) <= Strong p where
```

```
  first :: ∀ a b c. p a b -> p (Tuple a c) (Tuple b c)
```

```
  second :: ∀ a b c. p b c -> p (Tuple a b) (Tuple a c)
```

```
class (Profunctor p) <= Choice p where
```

```
  left :: ∀ a b c. p a b -> p (Either a c) (Either b c)
```

```
  right :: ∀ a b c. p b c -> p (Either a b) (Either a c)
```

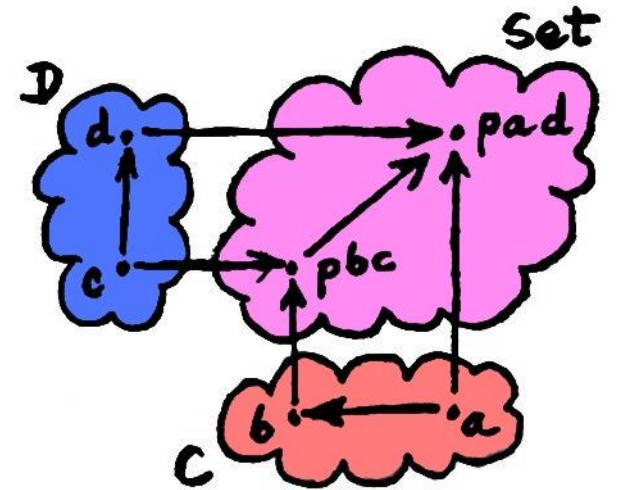
```
newtype Star f a b = Star (a -> f b)
```

```
instance profunctorStar :: (Functor f) => Profunctor (Star f) where
```

```
  dimap f g (Star ft) = Star (f >>> ft >>> map g)
```

```
class (Strong p, Choice p) <= Wander p where
```

```
  wander :: ∀ s t a b. (∀ f. (Applicative f) => (a -> f b) -> s -> f t)
    -> p a b -> p s t
```



Approach #3 – Profunctor

```
type Optic p s t a b = p a b -> p s t
```

```
type Iso s t a b =  $\forall$  p. (Profunctor p) => Optic p s t a b
```

```
type Lens s t a b =  $\forall$  p. (Strong p) => Optic p s t a b
```

```
type Prism s t a b =  $\forall$  p. (Choice p) => Optic p s t a b
```

```
type Traversal s t a b =  $\forall$  p. (Wander p) => Optic p s t a b
```

```
type Fold r s t a b = Optic (Star (Const r)) s t a b
```

Usage - UI

- UI is a profunctor (actually a monad ☹)
- Components access a local view model
- Child components can be embedded in a bigger component using lenses and traversals that focus on the respective sub-states
- Components provide a handler function that, given a new state, triggers an update of the UI and generates a view that is finally rendered using virtual-dom

Other usages

- Monomorphic containers
- DB views
- GADTs
- ...

Links

- <http://www.janis-voigtlaender.eu/papers/ThreeComplementaryApproachesToBidirectionalProgramming.pdf>
- <http://www.seas.upenn.edu/~harmony/>
- <http://artyom.me/lens-over-tea-1>
- <http://zrho.me/posts/2015-08-23-optic-ui.html>
- <http://www.haskellforall.com/2015/10/explicit-is-better-than-implicit.html>